#### IN THIS CHAPTER, YOU WILL LEARN:

- how to incorporate technological progress in the Solow model
- about policies to promote growth
- about growth empirics: confronting the theory with facts
- two simple models in which the rate of technological progress is endogenous

#### Introduction

In the Solow model of Chapter 8,

- the production technology is held constant.
- income per capita is constant in the steady state.

Neither point is true in the real world:

- 1900–2013: U.S. real GDP per person grew by a factor of 8.3, or 1.9% per year.
- examples of technological progress abound (see next slide).

### **Examples of technological progress**

- U.S. farm sector productivity nearly tripled from 1950 to 2012.
- The real price of computer power has fallen an average of 30% per year over the past three decades.
- 2000: 361 million Internet users, 740 million cell phone users
   2015: 3.1 billion Internet users, 4.9 billion cell phone users
- 2001: iPod capacity = 5gb, 1000 songs. Not capable of playing episodes of Game of Thrones.
  - 2015: iPod touch capacity = 64gb, 16,000 songs. Can play episodes of *Game of Thrones*.

- A new variable: *E* = labor efficiency
- Assume:

Technological progress is **labor-augmenting**: it increases labor efficiency at the exogenous rate *g*:

$$oldsymbol{g} = rac{\Delta oldsymbol{\mathcal{E}}}{oldsymbol{\mathcal{E}}}$$

We now write the production function as:

$$Y = F(K, L \times E)$$

- where L × E = the number of effective workers.
  - Increases in labor efficiency have the same effect on output as increases in the labor force.

Notation:

Production function per effective worker:

$$y = f(k)$$

Saving and investment per effective worker:

$$sy = sf(k)$$

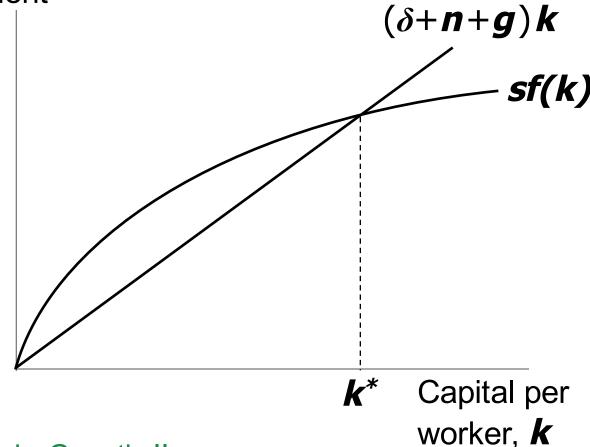
 $(\delta + n + g)k$  = break-even investment: the amount of investment necessary to keep k constant.

#### Consists of:

- $\bullet$   $\delta$  k to replace depreciating capital
- nk to provide capital for new workers
- gk to provide capital for the new "effective" workers created by technological progress

Investment, break-even investment

$$\Delta \mathbf{k} = \mathbf{s} \, \mathbf{f}(\mathbf{k}) \, - (\delta + \mathbf{n} + \mathbf{g}) \mathbf{k}$$



# Steady-state growth rates in the Solow model with tech. progress

Variable	Symbol	Steady-state growth rate
Capital per effective worker	$k = K/(L \times E)$	0
Output per effective worker	$y = Y/(L \times E)$	0
Output per worker	$(Y/L) = y \times E$	g
Total output	$Y = y \times E \times L$	n + g

# The Golden Rule with technological progress

To find the Golden Rule capital stock, express  $c^*$  in terms of  $k^*$ :

$$c^* = y^* - i^*$$
$$= f(k^*) - (\delta + n + g)k^*$$

c\* is maximized when

$$MPK = \delta + n + g$$

or equivalently,

$$MPK - \delta = n + g$$

In the Golden
Rule steady state,
the marginal
product of capital
net of depreciation
equals the
pop. growth rate
plus the rate of
tech progress.

### **Growth empirics: Balanced growth**

- Solow model's steady state exhibits balanced growth—many variables grow at the same rate.
  - Solow model predicts Y/L and K/L grow at the same rate (g), so K/Y should be constant.
     This is true in the real world.
  - Solow model predicts real wage grows at same rate as Y/L, while real rental price is constant.
     Also true in the real world.

- Solow model predicts that, other things equal, poor countries (with lower Y/L and K/L) should grow faster than rich ones.
- If true, then the income gap between rich & poor countries would shrink over time, causing living standards to converge.
- In real world, many poor countries do NOT grow faster than rich ones. Does this mean the Solow model fails?

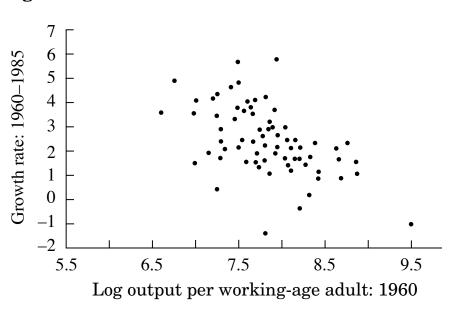
- Solow model predicts that, other things equal, poor countries (with lower Y/L and K/L) should grow faster than rich ones.
- No, because "other things" aren't equal:
  - In samples of countries with similar savings & pop. growth rates, income gaps shrink about 2% per year.
  - In larger samples, after controlling for differences in saving, pop. growth, and human capital, incomes converge by about 2% per year.

- What the Solow model really predicts is conditional convergence—countries converge to their own steady states, which are determined by saving, population growth, and education.
- This prediction comes true in the real world.

Figure 1



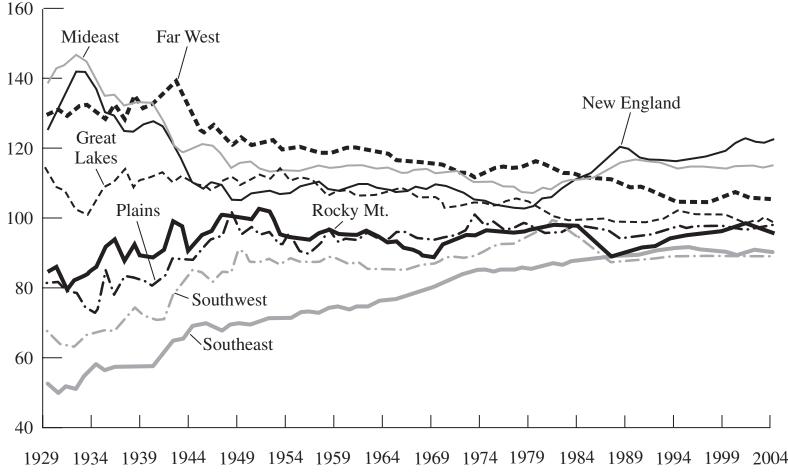
Figure 2



Source: Figures 1 and 2: G. Mankiw, D. Romer, and D. Weil, "A Contribution to the Empirics of Economic Growth," Quarterly Journal of Economics 107, no. 2 (May 1992): 407–38.

See Supplement 9-1.

Per Capita Personal Income as a Percentage of U.S. Average By Region Figure 1



Source: U.S. Department of Commerce, Bureau of Economic Analysis.

See Supplement 9-2.

## Growth empirics: Factor accumulation vs. production efficiency

- Differences in income per capita among countries can be due to differences in:
  - 1. capital—physical or human—per worker
  - 2. the efficiency of production (the height of the production function)
- Studies:
  - Both factors are important.
  - The two factors are correlated: countries with higher physical or human capital per worker also tend to have higher production efficiency.

## Growth empirics: Factor accumulation vs. production efficiency

- Possible explanations for the correlation between capital per worker and production efficiency:
  - Production efficiency encourages capital accumulation.
  - Capital accumulation has externalities that raise efficiency.
  - A third, unknown variable causes capital accumulation and efficiency to be higher in some countries than others.

### **Policy issues**

- Are we saving enough? Too much?
- What policies might change the saving rate?
- How should we allocate our investment between privately owned physical capital, public infrastructure, and human capital?
- How do a country's institutions affect production efficiency and capital accumulation?
- What policies might encourage faster technological progress?

- Use the Golden Rule to determine whether the U.S. saving rate and capital stock are too high, too low, or about right.
  - If  $(MPK \delta) > (n + g)$ , U.S. economy is below the Golden Rule steady state and should increase s.
  - If  $(MPK \delta) < (n + g)$ , U.S. economy is above the Golden Rule steady state and should reduce s.

To estimate  $(MPK - \delta)$ , use three facts about the U.S. economy:

- k = 2.5 y
   The capital stock is about 2.5 times one year's GDP.
- 2.  $\delta \mathbf{k} = 0.1 \, \mathbf{y}$ About 10% of GDP is used to replace depreciating capital.
- 3.  $MPK \times k = 0.3 y$ Capital income is about 30% of GDP.

1. 
$$k = 2.5 y$$

2. 
$$\delta k = 0.1 y$$

3. 
$$MPK \times k = 0.3 y$$

To determine  $\delta$ , divide 2 by 1:

$$\frac{\delta k}{k} = \frac{0.1 y}{2.5 y} \implies \delta = \frac{0.1}{2.5} = 0.04$$

1. 
$$k = 2.5 y$$

2. 
$$\delta k = 0.1 y$$

3. 
$$MPK \times k = 0.3 y$$

To determine MPK, divide 3 by 1:

$$\frac{\mathsf{MPK} \times \mathbf{k}}{\mathbf{k}} = \frac{0.3 \, \mathbf{y}}{2.5 \, \mathbf{y}} \implies \mathsf{MPK} = \frac{0.3}{2.5} = 0.12$$

Hence,  $MPK - \delta = 0.12 - 0.04 = 0.08$ 

- From the last slide:  $MPK \delta = 0.08$
- U.S. real GDP grows an average of 3% per year, so n + g = 0.03
- Thus,  $MPK \delta = 0.08 > 0.03 = n + g$
- Conclusion:

The U.S. is below the Golden Rule steady state: Increasing the U.S. saving rate would increase consumption per capita in the long run.

### Policy issues: How to increase the saving rate

- Reduce the government budget deficit (or increase the budget surplus).
- Increase incentives for private saving:
  - Reduce capital gains tax, corporate income tax, estate tax, as they discourage saving.
  - Replace federal income tax with a consumption tax.
  - Expand tax incentives for IRAs (individual retirement accounts) and other retirement savings accounts.

# Policy issues: Allocating the economy's investment

- In the Solow model, there's one type of capital.
- In the real world, there are many types, which we can divide into three categories:
  - private capital stock
  - public infrastructure
  - human capital: the knowledge and skills that workers acquire through education
- How should we allocate investment among these types?

# Policy issues: Allocating the economy's investment

#### Two viewpoints:

1. Equalize tax treatment of all types of capital in all industries, then let the market allocate investment to the type with the highest marginal product.

#### 2. Industrial policy:

Government should actively encourage investment in capital of certain types or in certain industries, because they may have positive externalities that private investors don't consider.

# Possible problems with industrial policy

- The government may not have the ability to "pick winners" (choose industries with the highest return to capital or biggest externalities).
- Politics (e.g., campaign contributions) rather than economics may influence which industries get preferential treatment.

# Policy issues: Establishing the right institutions

- Creating the right institutions is important for ensuring that resources are allocated to their best use. Examples:
  - Legal institutions, to protect property rights.
  - Capital markets, to help financial capital flow to the best investment projects.
  - A corruption-free government, to promote competition, enforce contracts, etc.

### **Establishing the right institutions: North vs. South Korea**

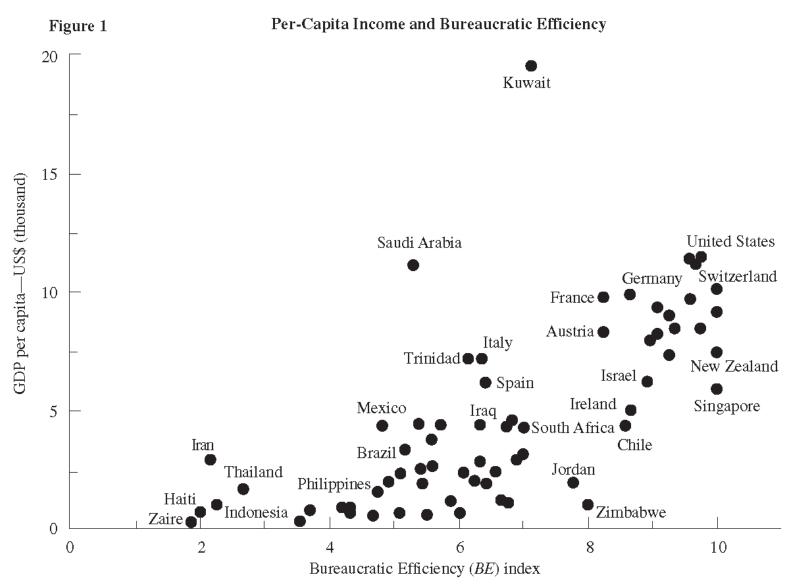
After WW2, Korea split into:

- North Korea with institutions based on authoritarian communism
- South Korea with Western-style democratic capitalism

Today, GDP per capita is over 10x higher in S. Korea than N. Korea



### **Establishing the right institutions: Corruption and Growth**



### Policy issues: Encouraging tech. progress

- Patent laws: encourage innovation by granting temporary monopolies to inventors of new products.
- Tax incentives for R&D
- Grants to fund basic research at universities
- Industrial policy: encourages specific industries that are key for rapid tech. progress (subject to the preceding concerns).

### **CASE STUDY: Is free trade good for economic growth?**

- Since Adam Smith, economists have argued that free trade can increase production efficiency and living standards.
- Research by Sachs & Warner:

Average annual growth rates, 1970–89			
	open	closed	
developed nations	2.3%	0.7%	
developing nations	4.5%	0.7%	

### **CASE STUDY: Is free trade good for economic growth?**

- To determine causation, Frankel and Romer exploit geographic differences among countries:
  - Some nations trade less because they are farther from other nations, or landlocked.
  - Such geographical differences are correlated with trade but not with other determinants of income.
  - Hence, they can be used to isolate the impact of trade on income.
- Findings: increasing trade/GDP by 2% causes
   GDP per capita to rise 1%, other things equal.

#### **Endogenous growth theory**

- Solow model:
  - sustained growth in living standards is due to tech progress.
  - the rate of tech progress is exogenous.
- Endogenous growth theory:
  - a set of models in which the growth rate of productivity and living standards is endogenous.

#### The basic model

- Production function: Y = AK where A is the amount of output for each unit of capital (A is exogenous & constant)
- Key difference between this model & Solow:
  MPK is constant here, diminishes in Solow
- Investment: sY
- Depreciation: δK
- Equation of motion for total capital:

$$\Delta K = sY - \delta K$$

#### The basic model

$$\Delta K = sY - \delta K$$

Divide through by K and use Y = AK to get:

$$\frac{\Delta Y}{Y} = \frac{\Delta K}{K} = sA - \delta$$

- If  $sA > \delta$ , then income will grow forever, and investment is the "engine of growth."
- Here, the permanent growth rate depends on s. In Solow model, it does not.

## Does capital have diminishing returns or not?

- Depends on definition of capital.
- If capital is narrowly defined (only plant & equipment), then yes.
- Advocates of endogenous growth theory argue that knowledge is a type of capital.
- If so, then constant returns to capital is more plausible, and this model may be a good description of economic growth.

#### A two-sector model

- Two sectors:
  - manufacturing firms produce goods.
  - <u>research</u> universities produce knowledge that increases labor efficiency in manufacturing.
- u = fraction of labor in research(u is exogenous)
- Manufacturing: Y = F[K, (1 u)EL]
- Research:  $\Delta E = g(u)E$
- Capital accumulation:  $\Delta K = sY \delta K$

#### A two-sector model

- In the steady state, manufacturing output per worker and the standard of living grow at rate  $\Delta E/E = g(u)$ .
- Key variables:
  - s: affects the level of income, but not its growth rate (same as in Solow model)
  - u: affects level and growth rate of income

#### **Facts about R&D**

- 1. Much research is done by firms seeking profits.
- 2. Firms profit from research:
  - Patents create a stream of monopoly profits.
  - Extra profit from being first on the market with a new product.
- 3. Innovation produces externalities that reduce the cost of subsequent innovation.

Much of the new endogenous growth theory attempts to incorporate these facts into models to better understand technological progress.

## Is the private sector doing enough R&D?

- The existence of positive externalities in the creation of knowledge suggests that the private sector is not doing enough R&D.
- But, there is much duplication of R&D effort among competing firms.
- Estimates: Social return to R&D ≥ 40% per year.
- Thus, many believe govt should encourage R&D.

### **Economic growth as "creative destruction"**

- Schumpeter (1942) coined term "creative destruction" to describe displacements resulting from technological progress:
  - the introduction of a new product is good for consumers but often bad for incumbent producers, who may be forced out of the market.
- Examples:
  - Luddites (1811–12) destroyed machines that displaced skilled knitting workers in England.
  - Walmart displaces many mom-and-pop stores.

#### CHAPTER SUMMARY

- 1. Key results from Solow model with tech progress:
  - Steady-state growth rate of income per person depends solely on the exogenous rate of tech progress
  - The U.S. has much less capital than the Golden Rule steady state
- 2. Ways to increase the saving rate
  - Increase public saving (reduce budget deficit)
  - Tax incentives for private saving

#### CHAPTER SUMMARY

#### 3. Empirical studies

- Solow model explains balanced growth, conditional convergence.
- Cross-country variation in living standards is due to differences in cap. accumulation and in production efficiency.
- 4. Endogenous growth theory: Models that
  - examine the determinants of the rate of tech. progress, which Solow takes as given.
  - explain decisions that determine the creation of knowledge through R&D.